Dynamic diagnosis of structures using a modal hammer and a dynamic inertance function

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ABSTRACT

As engineers, we do expertises on structural condition of structures, when damages occur on them. Simple look at a damaged pattern allows us some times to evaluate safety of it and detect reasons of observed damages and deformations. In most cases, especially related to historical structures, simple optical survey and engineering experience is not enough. We have to use more or less complicated diagnosis tools (laboratory and in situ test on material properties, geometry survey, dynamic and foundation investigation or analysis of numerical models) and to engage a large team of various experts (in very complex cases). Additionally in historical structures, knowledge about past reconstructions and structural interventions is required, where an expert has to behave like a detective to discover real danger and needs requiring a proper structural intervention. Often, a bad structural condition of an analysed structure is unknown and sudden collapse without any warning happens, as in the case of the Pavia Civil Tower in Italy.

Presently, quick development of diagnostic methods and measurement systems allows us to do very sophisticated diagnosis but it is rather costly, complex and in some cases impossible action. Being on site, an expert need simple and handy tool, offering in analysis wide spectrum of useful information. Dynamic modal analysis of structures allows engineers for powerful diagnosis, when proper methods are used. One of such powerful method is analysis of dynamic inertance and compliance functions, determined with a modal hammer. This simple tool can be easily used on site for testing of structures and structural elements. Acquired data can be analysed in laboratory and elaborated results allow detecting changes in eigen-frequency and thus in global or local structural stiffness. This information is significant when structural eigen-frequencies start to be close to the dominant frequency band characteristic for a seismic area. Threatened of resonance, assessed during dynamic monitoring of a structure, should trigger structural intervention process to avoid sudden collapse of urban and heritage structures during next earthquake. The presented diagnostic methodology allows also determining damping of the structure, which both with eigen-frequencies can be useful for validation of numerical models of structures. Properly validated numerical models allow engineers to assess more easy vulnerability and toughness of analysed structures. This diagnosis methodology is presented on structural examples, examined also on a shake table.

Assessment of heritage structures using a modal hammer and dynamic inertance and compliance functions allow for periodic control (monitoring) of changing structural properties, which can be used in an object passport collecting proper information for authorities and owners.

Highlights

- Diagnosis method simple in use on site
- Detection of stiffness changes of a damaged (cracked) structure
- Determination of dynamic properties of structures
- Evaluation method suitable for structures in seismic areas.

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1985 – 1990: Structural Engineering Technician, Secondary School of Structural Engineering

Work experience:

since 2020: Member of the Interdisciplinary Committee for repair of historical masonry arch viaduct in Cracow.

2019-20: Task coordinator in the project INMASPOL "INfills and MASonry structures protected by deformable POLyurethanes in seismic areas" realized in frame of the SERA — H2020-INFRAIA-2016-2017/H2020-INFRAIA-2016-1 "Seismology and Earthquake Engineering Research Infrastructure Alliance for Europe"

2017-20: Member of the POIR.04.01.02-00-0016/17-00 project (EU funds) "Innovative technology of vibro-acoustic insulation of floors"

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2018: ISCARSAH Expert for assessment of structural condition of heritage structures in Iran

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Department (on applications of polymer flexible joints)

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2014-15: Member of the Organizing Committee of the 70th Anniversary of the Cracow University of Technology (Forum: *Science and Economy*; Anniversary Scientific Conference: *Practical applications of innovative solutions resulting from scientific research*)

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	 Polish Scientific Research Committee 1996 – 2020: Several dozen expert opinions on the construction condition of buildings and on the behaviour of structures under static and dynamic excitations 1996 – 2005: Projects of strengthening of historical masonry building in Cracow - including FRP materials (the first strengthening project of the brick arches in Poland /in 1998/ with realization in 2002) 1997 – 2012: Calculations of concrete chimneys 1999: Member of the Organizing Committee the 19th International Meeting in Cracow of the International Association of Spatial Structures since 1993: Working with computer programs: MS Office (Word, Excel, Power Point), AUTOCAD, MATHCAD, other engineering programs.
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